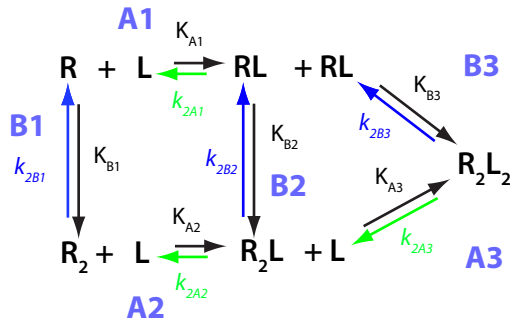


B-R2-R2L2

Receptor dimerization coupled with binding of one ligand per receptor monomer

Macroscopic reaction scheme



Thermodynamic cycle

$$\Delta G_{B1}^{\circ} + \Delta G_{A2}^{\circ} = \Delta G_{A1}^{\circ} + \Delta G_{B2}^{\circ} \Rightarrow K_{B1} K_{A2} = K_{A1} K_{B2}$$

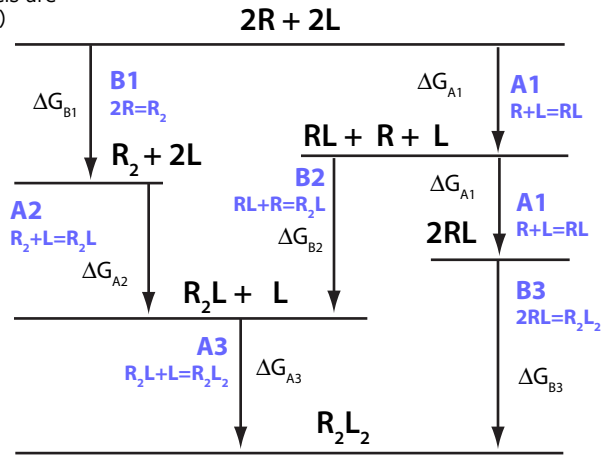
$$\Delta G_{B1}^{\circ} + \Delta G_{A2}^{\circ} + \Delta G_{A3}^{\circ} = 2\Delta G_{A1}^{\circ} + \Delta G_{B3}^{\circ} \Rightarrow K_{B1} K_{A2} K_{A3} = K_{A1}^2 K_{B3}$$

Dependent transitions: B2 and B3

$$K_{B2} = K_{A2} K_{B1} / K_{A1}$$

$$K_{B3} = K_{B1} K_{A2} K_{A3} / K_{A1}^2$$

Free-energy diagram
(positions of energy levels are chosen for easy viewing)



Microscopic reaction scheme

By symmetric design of the model:

$$\Delta G_{B2a}^{\circ} = \Delta G_{B2b}^{\circ}, K_{B2a} = K_{B2b} = K_{B2m} \text{ (microscopic)}$$

$$\Delta G_{A2a}^{\circ} = \Delta G_{A2b}^{\circ}, K_{A2a} = K_{A2b} = K_{A2m}$$

$$\Delta G_{A3a}^{\circ} = \Delta G_{A3b}^{\circ}, K_{A3a} = K_{A3b} = K_{A3m}$$

The same holds for kinetic constants.

Thermodynamic cycles:

$$\Delta G_{B1}^{\circ} + \Delta G_{A2a}^{\circ} = \Delta G_{A1}^{\circ} + \Delta G_{B2a}^{\circ}$$

$$\Delta G_{B1}^{\circ} + \Delta G_{A2b}^{\circ} = \Delta G_{A1}^{\circ} + \Delta G_{B2b}^{\circ}$$

$$K_{B1} K_{A2m} = K_{A1} K_{B2m}$$

$$\Delta G_{B2b}^{\circ} + \Delta G_{A3b}^{\circ} = \Delta G_{A1}^{\circ} + \Delta G_{B3}^{\circ}$$

$$K_{B2m} K_{A3m} = K_{A1} K_{B3}$$

Dependent transitions: B2 and B3

$$K_{B2m} = K_{B1} K_{A2m} / K_{A1}$$

$$K_{B3} = K_{B1} K_{A2m} K_{A3m} / K_{A1}^2$$

