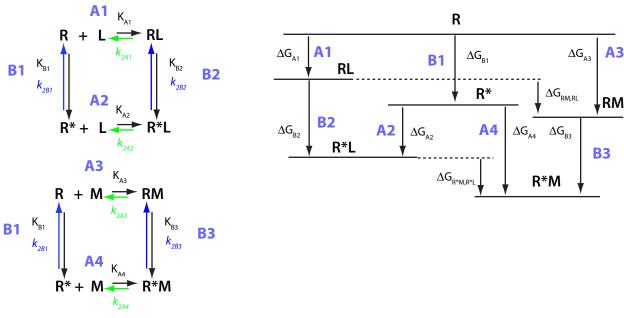
U-R-RL-RM

Binding of two mutually exclusive ligands coupled with intramolecular isomerization of the receptor (competitive ligand binding)

Reaction scheme

Free-energy diagram (positions of energy levels are chosen for easy viewing)



Thermodynamic cycles

$$\Delta G^{\circ}_{B1} + \Delta G^{\circ}_{A2} = \Delta G^{\circ}_{A1} + \Delta G^{\circ}_{B2} , \qquad K_{B1} K_{A2} = K_{A1} K_{B2}$$
$$\Delta G^{\circ}_{B1} + \Delta G^{\circ}_{A4} = \Delta G^{\circ}_{A3} + \Delta G^{\circ}_{B3} , \qquad K_{B1} K_{A4} = K_{A3} K_{B3}$$

For calculations I will assume that I know equilibrium constants for B1, B2, B3, A1 and A3. Dependent constants then correspond to A2 and A4:

$$\begin{array}{l} {\sf K}_{{}_{{\rm A}2}}{=}\,{\sf K}_{{}_{{\rm A}1}}{\sf K}_{{}_{{\rm B}2}}\!/{\sf K}_{{}_{{\rm B}1}} \\ {\sf K}_{{}_{{\rm A}4}}{=}\,{\sf K}_{{}_{{\rm A}3}}{\sf K}_{{}_{{\rm B}3}}\!/{\sf K}_{{}_{{\rm B}1}} \end{array}$$

Additional equilibrium constants between alternative forms of R and R* may be determined as:

Relationship between concentrations of bound forms of R:

$$\begin{split} & \kappa_{_{RM,RL}} \! = \! [RM][L] \, / \{[RL][M]\} \\ & \Delta G^{\circ}_{_{A3}} - \Delta G^{\circ}_{_{A1}} = \Delta G^{\circ}_{_{RM,RL}} \\ & \kappa_{_{RM,RL}} \! = \! \kappa_{_{A3}} \! / \kappa_{_{A1}} \end{split}$$

Relationship between concentrations of bound forms of R*:

$$\begin{array}{l} K_{R^*M,R^*L} = [R^*M][L] \ / \{[R^*L][M]\} \\ \Delta G^{\circ}_{A3} \ + \ \Delta G^{\circ}_{B3} \ - \ \Delta G^{\circ}_{A1} \ - \ \Delta G^{\circ}_{B2} \ = \ \Delta G^{\circ}_{R^*M,R^*L} \\ K_{R^*M,R^*L} = K_{A3} K_{B3} / (K_{A1} K_{B2}) \end{array}$$